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# Degradation in Performance of Adaptive Null-Steering Antennas

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Airborne Radar Branch Radar Division

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### DEGRADATION IN PERFORMANCE OF ADAPTIVE **NULL-STEERING ANTENNAS**

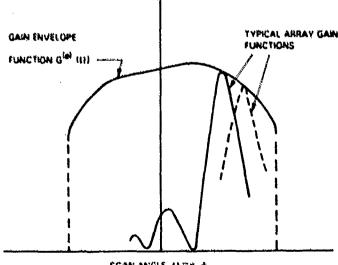
#### INTRODUCTION

This report quantifies the degradation in the overall main beam gain performance capability of any phased array antenna which necessarily accompanies the formation of pattern nulls in a number of directions. The adaptive formation of pattern nulls constitutes one strategy through which a radar may seek to suppress effects of stand-off jammers. However, an array comprising a finite number of elementary radiators disposes of only a finite number of degrees of freedom. Thus it has long been recognized that as the number of nulls required approaches the number of degrees of freedom, antenna performance deteriorates. Here, this fact is given a simple quantitative formulation very much in accord with our intuitive expectation.

#### **PERFORMANCE**

The primary function of a phased array antenna is to form a high-gain beam along any direction within some (limited) scan volume. From this standpoint, the performance of a phased array is summarized by the envelope gain function of the array  $G_{max}(\Omega)$ ; other pattern characteristics such as (peak) sidelobe level are not considered here. This function specifies the maximum realizable gain from the complete array in any given direction  $\Omega \equiv (\theta, \phi)$ , when the elements of the array are excited by real generators matched to their waveguide leads with optimum amplitude and phase for gain in that particular direction. The envelope gain function is, of course, quite different from the conventional array gain-pattern function corresponding to any one particular scan angle, i.e., fixed distribution of excitation. Figure 1 contrasts the gain envelope and conventional gain-pattern functions. Under certain conditions, we can relate the number of antenna elements in the array and array performance as specified by the envelope gain function [1,2].

Fig. 1 - Schematic representation of gain-envelope function and typical antenna array gain functions for fixed scan angles (fixed excitation)



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We assume the elementary antennas of the array to be essentially lossless (Lorentz) reciprocal components; dissipation occurs only in the internal impedance loads of the generators exciting each antenna (or feed network). See Fig. 2. Further, we shall assume that at any given operating frequency:

- a fixed total available power can be distributed arbitrarily among the individual radiating elements;
- each element is equipped with a phase shifter;
- in any given direction, all elementary antennas radiate fields with the same polarization.

The last assumption permits us to use scalar theory. Although there is no requirement that all the elementary antennas be otherwise similar, this is normally the case. This then assures that the third assumption is satisfied, at least to first order. The third assumption is valid exactly if the elementary antennas have identical field patterns in the open-circuited array environment.

Under the foregoing conditions, we may show [see appendix] that

$$N = \frac{1}{\eta} \frac{1}{4\pi} \int \int G_{\text{max}}^{(e)}(\Omega') d\Omega', \qquad (2.1)$$

scan volume

where

N is the number of elements in the array;

η is the average element efficiency;

 $G_{\max}^{(e)}(\Omega)$  is the maximal gain-envelope function;

 $\Omega$  is the bearing in space equivalent to the spherical coordinates  $\theta, \phi$ ; and

 $d\Omega$  is the differential element of solid angle (sin  $\theta$ )  $d\theta$   $d\phi$ .

The average element efficiency [3,4] is given by

$$\eta = \frac{1}{N} \sum \eta_m, \tag{2.2}$$

where  $\eta_m$ , the efficiency associated with the *m*th element of the array, is the ratio of the power radiated from the entire array when only the *m*th element is excited to the power available from the generator exciting that *m*th element.

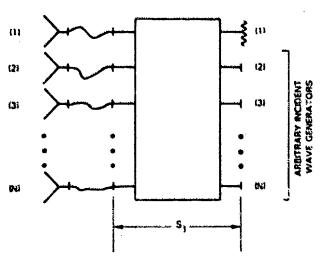


Fig. 2.— Arbitrary incident wave excitation at N=1 ports of the transparent feed network S maintains the null in direction  $\Omega_1$ 

The element efficiency just defined is a measure of mutual coupling.

$$\eta_{m} = \frac{P_{m} \text{ (radiated)}}{P_{m} \text{ (available)}} = \frac{P_{m} \text{ (available)} - P_{m} \text{ (reflected)}}{P_{m} \text{ (available)}},$$

$$= 1 - \sum_{n=1}^{N} |S_{nm}|^{2}.$$
(2.3)

The coefficients  $S_{nm}$  are the normalized scattering coefficients describing coupling among the elements of the array.

$$b_n = \sum_{m=1}^{N} S_{nm} a_m {(2.4a)}$$

$$2\sqrt{R_g} a_m = V_m + Z_g I_m {2.4b}$$

$$2\sqrt{R_g}\,b_m = V_m - Z_g^*\,I_m \tag{2.4c}$$

$$Z_g = R_g + jX_g. ag{2.4d}$$

Evidently the stronger the mutual coupling the smaller the element efficiency  $\eta$ . The smaller the element efficiency, the larger is the number of antenna array elements N required for a given gain envelope performance. It is remarkable that the number of antenna elements required does not explicitly depend on the gain functions of these individual array elements, and (since  $\eta \leq 1$ ) that there exists an absolute minimum value of N.

#### EFFECT OF THE NULL-FORMING CONSTRAINT

Consider a specified antenna array where the gain performance is summarized by the gain envelope function  $G_0^{(e)}(\Omega)$ . This particular array then must comprise N

$$N \geqslant \frac{1}{4\pi\eta} \int \int G_0^{(\epsilon)}(\Omega') d\Omega' \tag{3.1}$$

elementary antennas. We now propose to employ this relation, in reverse as it were, as a constraint governing the performance of the array under the assumption that the array must form nulls in certain prescribed directions.

Suppose that a radiation null is demanded in the direction  $\Omega_1 \equiv (\theta_1, \phi_1)$ . We will construct a transparent 2N-port network which, when connected in tandem with all the elements of the array, will effect the following result: arbitrary excitation of the array at N-1 of the input ports to this network will maintain the prescribed null. A lossless reciprocal 2N-port network has been termed "transparent" when waves incident at one set of N ports do not cause reflected waves to emerge at any of those N ports. Let  $f_n(\Omega_1)$  be proportional to (a component of) the far field in the direction  $\Omega_1$  obtained when the nth element of the original array is excited by a unit incident wave amplitude,  $a_n = 1$ , in the environment of all the remaining elements terminated in loads,  $Z_g$ .

If necessary, we add lengths of transmission line at any port so that the generally complex quantities  $f_n^{(1)}(\Omega_1)$  are all real and positive. The  $f_n^{(1)}(\Omega_1)$  can be ordered into a column vector  $\mathbf{f}^{(1)}(\Omega_1)$  denotes the transpose):

$$\tilde{\mathbf{f}}^{(1)} = \left[ f_1^{(1)}(\Omega_1) f_2^{(1)}(\Omega_1) \dots f_N^{(1)}(\Omega_1) \right]. \tag{3.2}$$

As shown in the appendix, an excitation of the array with incident wave amplitudes proportional to  $f^{(1)}$  realizes the maximum gain in the direction  $\Omega_1$  obtainable with given array and given real generators. Any excitation of the array orthogonal to  $f^{(1)}$  preserves a null in the direction  $\Omega_1$ .

The transparent network that physically separates out N-1 ports that may be excited by arbitrary incident waves without disturbing the null in the direction  $\Omega_1$  is constructed as follows. Form the vector

$$\mathbf{h}_{1}^{(1)} = \mathbf{f}^{(1)} \left( \tilde{\mathbf{f}}^{(1)} \mathbf{f}^{(1)} \right)^{-1}. \tag{3.3}$$

By means of the Gram-Schmidt process, provide N-1 additional orthornormal vectors  $\mathbf{h}_2^{(1)}$ ,  $\mathbf{h}_3^{(1)}$ , ...,  $\mathbf{h}_N^{(1)}$  spanning the subspace orthogonal to  $\mathbf{h}_1^{(1)}$ , and define the transformation matrix

$$T_1 = \left[ \mathbf{h}_1^{(1)} \ \mathbf{h}_2^{(1)} \dots \mathbf{h}_N^{(1)} \right]. \tag{3.4}$$

The scattering matrix

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$$S_{1} = \begin{bmatrix} 0 & | & \bar{T}_{1} \\ -\frac{1}{T_{1}} & | & 0 \end{bmatrix}$$
 (3.5)

then clearly represents a lossless reciprocal 2N-port which, on account of the properties associated with zero submatrices on the principal diagonal, has been termed "transparent." Ports N+1 to 2N are to be connected to antenna elements 1 to N, respectively. By this construction, shown in Fig. 2, arbitrary excitations of ports 2 to N of the transparent network (i.e., no excitation at port 1) will preserve the required null.

Using the realized gain functions corresponding to excitation of these same ports 2 to N, we compute a modified gain-envelope function

$$G_1^{(e)}(\Omega) \leqslant G_0^{(e)}(\Omega). \tag{3.6}$$

The essence of this analysis is to observe that this new gain envelope function must satisfy the integral constraint

$$N-1 \geqslant \frac{1}{4\pi\eta} \int\!\!\int G_1^{(p)}(\Omega') d\Omega'. \tag{3.7}$$

scan volume

It is important to observe that  $\eta \leq 1$ , which accounts for the mutual coupling present in the originally specified array, is unaffected (invariant) when the array is cascaded with a *transparent 2N*-port network. This is demonstrated in the appendix of this report.

Suppose now that in addition a second null, in the direction  $\Omega_2 \equiv (\theta_2, \phi_2)$  is required. Let  $f_A^{(2)}(\Omega_2)$  be proportional to a component of the far field radiated in the direction  $\Omega_2$  when the *n*th port of the transparent network found above (Fig. 2) is excited by a unit incident wave amplitude.

If necessary, we again add lengths of transmission line at any port such that the generally complex quantities  $f_n^{(2)}(\Omega_3)$  are all real and positive. It is possible (though unlikely) that

$$\left[f_1^{(n)}(\Omega_2) f_2^{(n)}(\Omega_2) \dots f_8^{(n)}(\Omega_8)\right] \tag{3.8}$$

is of the form

$$\left[f_1^{(2)}(\Omega_2) \mid 0 \mid \mid 0 \mid \dots \mid 0\right].$$

i.e., a null in the direction  $\Omega_2$  is automatically assured by excluding excitation at port 1.

In the more likely general circumstance,

$$\tilde{f}^{(1)} = \left[ 0 \ f_1^{(2)} \ (\Omega_2) \ f_2^{(2)} \ (\Omega_3) \dots f_n^{(n)} \ (\Omega_2) \right] \tag{3.9}$$

is not the zero vector, and excitation proportional to  $f^{(2)}$  realizes the gain  $G_1^{(c)}(\Omega_2)$  in the direction  $\Omega_2$ .

We now form the vector

$$\mathbf{h}^{(2)} = \mathbf{f}^{(2)} \ (\tilde{\mathbf{f}}^{(2)}\mathbf{f})^{-1}.$$
 (3.10)

Using the Gram-Schmidt process, we again provide N-2 additional orthonormal vectors  $\mathbf{h}_1^{(2)}, \mathbf{h}_3^{(2)}, \ldots, \mathbf{h}_N^{(2)}$  spanning the subspace orthogonal to that spanned by  $\mathbf{h}_1^{(1)}$ ,  $\mathbf{h}_2^{(2)}$ , and define the transformation matrix

$$T_2 = [\delta_1 \ h_2^{(2)} \ h_3^{(2)} \ \dots \ h_N^{(2)}].$$
 (3.11)

The vector  $\delta_n$  has an *n*th element equal to unity, and all other elements are zero. The scattering matrix

$$S_2 = \begin{bmatrix} 0 & \tilde{T}_2 \\ -T_2 & 0 \end{bmatrix}$$
 (3.12)

represents a transparent 2N-port network. Actually 2N-port notation is retained only for convenience in bookkeeping associated with port numbers. The  $\tilde{\delta}_1$  row and  $\delta_1$  column appearing in  $\tilde{T}_2$  and  $T_2$  are simply interpreted as requiring no further connection to port number 1 of the first transparent 2N-port. Effectively, a new 2(N-1) port is connected to the array. Figure 3 shows the result. By construction, arbitrary excitation of ports 3 to N of the second transparent network (i.e., no excitation at ports 1 and 2) will preserve the required two nulls. Using the realized gain functions corresponding to excitations of these N-2 ports, we compute a further modified gain envelope function

$$G_{i}^{(\epsilon)}(\Omega) \leqslant G_{i}^{(\epsilon)}(\Omega) \tag{3.13}$$

that satisfies the constraint

$$N-2 \geqslant \frac{1}{4\pi\eta} \int \int G_2^{(e)}(\Omega') d\Omega'. \tag{3.14}$$

scan volume

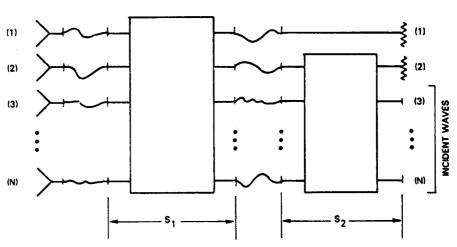


Fig. 3 — Arbitrary incident wave excitation at N-2 ports of the transparent feed network  $S_2$  maintains the nulls in directions  $\Omega_1$  and  $\Omega_2$ 

Evidently this process can be repeated for additional prescribed nulls. Should it be repeated N times, the effect on array performance would clearly be catastrophic.

However, at every intermediate iteration of this process, the number of ports that can be excited while maintaining the prescribed (independent) nulls is reduced by one. Thus M independent prescribed nulls effectively reduces an N element array to an N-M array of elements (ports) that can

be arbitrarily excited. Consequently the gain envelope for the array, constrained to retain the prescribed nulls, must satisfy

$$N-M \geqslant \frac{1}{4\pi\eta} \int \int G_M^{(e)}(\Omega') d\Omega'. \tag{3.15}$$

scan volume

The gain envelope (performance)  $G_M^{(e)}$ , on the average, is therefore necessarily reduced relative to the performance attainable without null constraints (2.5).

#### CONCLUSION

It has been shown that the requirement for an N-element array antenna (adaptively) to form nulls in a number of directions  $\Omega_1, \Omega_2, \ldots, \Omega_M$ ,  $M \leq N$ , necessarily degrades the achievable performance on the average from the array. The qualification "on the average," of course, refers to the integral nature of the constraints (3.15).

#### **ACKNOWLEDGMENT**

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#### **Appendix**

## DEFINITION AND PHYSICAL SIGNIFICANCE OF ELEMENT EFFICIENCY

The efficiency of the mth elementary antenna within the environment of an entire array of N terminated lossless antenna elements may be defined [A1] as

$$\eta_m = \frac{P_m(\text{radiated})}{P_m(\text{available})} = 1 - \frac{P_m(\text{reflected})}{P_m(\text{available})}$$
(A1)

where  $P_m$  (radiated) is the power radiated into space when the *m*th element only is excited,  $P_m$  (available) is the power available at the *m*th element, and  $P_m$  (reflected) is the power reflected back into the single excited element plus the power reflected (coupled) into all the remaining array elements that are not excited. Since for power per steradian  $P(\Omega)$  at any angle bearing  $\Omega \rightarrow (\theta, \phi)$  the gain functions, the directive gain  $g_d$ , and the realized gain  $g_r$  are, respectively, [A1]

$$g_J(\Omega) = 4\pi \frac{P(\Omega)}{P(\text{radiated})},$$
 (A2a)

$$g_r(\Omega) = 4\pi \frac{P(\Omega)}{P(\text{avaliable})}$$
, (A2b)

and one has, for the mth element,

teres seeded the seed represent products of respective the senses and

$$\eta_{m} = \frac{g_{rm}(\Omega)}{g_{dm}(\Omega)}.$$
 (A3)

Finally, when the coupling among the elements of the array is described at some fixed frequency by a normalized scattering matrix  $S = \{S_{nm}\}$ , relating incident-wave amplitudes  $a_m$  to corresponding reflected-wave amplitudes  $b_n$  at each antenna port,

$$b_n = \sum_{m=1}^{N} S_{nm} a_m, \quad m = 1, 2, \dots, N$$
 (A4)

the efficiency of the mth element given in Eq. (A1) may be written as

$$\eta_m = 1 - \sum_{n=1}^{N} |x_{nm}|^2. \tag{A5}$$

The maximum gain attainable from the complete array in any given direction  $\Omega'$ , when elements are individually excited by matched generators in the optimal fashion to yield the maximum gain in that direction, is given in terms of realized gain of the individual elements (A2) by

$$G_{\max}(\Omega^{\gamma}) = \sum_{i=1}^{N} g_{im}(\Omega^{\gamma}),$$
 (A6)

This is most readily verified as follows. By definition the realized gain of the array in the direction  $\Omega_0$  is

$$G_{r}(\Omega_{0}) = \frac{\left|\sum_{m=1}^{N} f_{m}(\Omega_{0})a_{m}\right|^{2}}{P_{r}(\text{available})/4\pi},$$
(A7)

where the reference planes have been chosen so that the  $f_n(\Omega_0) = \sqrt{g_m(\Omega_0)}$  are real and positive. The numerator may be considered as the scalar product of two vectors  $\hat{\mathbf{f}} \cdot \mathbf{a}$  which is maximized when  $\mathbf{a}$  is parallel to  $\mathbf{f}$ . Setting

$$a_{m} = \alpha f_{m}(\Omega_{0}) \tag{A8}$$

we have

$$P \text{ (available)} = \sum_{m=1}^{N} |a_m|^2 = |\alpha|^2 \sum_{m=1}^{N} |f_m(\Omega_0)|^2.$$
 (A9)

Substituting in Eq. (A7) we obtain Eq. (A6). The mean value of Eq. (A6) averaged over all angles  $\Omega'$  in space yields

$$\frac{1}{4\pi} \int_{\text{sphere}} G_{\text{max}}(\Omega') d\Omega' = \sum_{m=1}^{N} \eta_m. \tag{A10}$$

Thus, in terms of the mean efficiency averaged over all the elements in the array [A2],

$$\eta = \frac{1}{N} \sum_{m=1}^{N} \eta_m \tag{A11}$$

one finds that

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$$N = \frac{1}{\eta} \frac{1}{4\pi} \iint_{\text{sphere}} G_{\text{max}}(\Omega') d\Omega'. \tag{A12}$$

This provides a valuable estimate of the number of antenna elements that are required to realize a desired "gain envelope" for an array. Although the actual value of  $\eta$  for a particular array may not be known, an upper bound may be established. Such upper bounds on  $\eta$ , termed "ideal" efficiencies  $\eta_i$ , have been computed for circular cylindrical arrays [A3] and various regular infinite linear and planar arrays [A1, A4]. In these two array configurations all elements occupy equivalent positions, and, therefore, by symmetry,  $\eta_m = \eta$ , for all m. The tabulated values of the bound  $\eta_i$  may be inserted in Eq. (A12) to obtain a minimum estimate for N.

Finally, if the array with scattering matrix  $S = \{S_{ma}\}$  is connected in tandem with a transparent 2N port

$$S = \begin{bmatrix} 0 & \frac{1}{T} & \frac{\tilde{T}}{1} \\ T & \frac{1}{T} & 0 \end{bmatrix} \tag{A13}$$

where T is a real orthogonal matrix,  $\tilde{T} = T^{-1}$ , then the scattering matrix at the input to the resulting network is  $S' = \tilde{T}ST$ . The average element efficiency  $\eta$  is given by the matrix expression (A2)

$$\eta = \frac{1}{N} \operatorname{trace} \{S^*S\}. \tag{A14}$$

where  $S^* = \tilde{S}^*$ . This trace is invariant under the transformation of S to S; in fact  $S^*S^* = (\tilde{T}ST)^*\tilde{T}ST = \tilde{T}S^*T\tilde{T}ST = 0.5$ .

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